

# **OWNER PREFERENCES REGARDING RENOVATION MEASURES – THE DEMONSTRATION OF USING MULTI-CRITERIA DECISION MAKING**

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**Abstract.** The article describes typical apartment buildings built in Swedish residential areas in the '50s, '60s and 70's. Each of these buildings included calculations on the effects and investment cost of a number of renovation measures aimed at improving energy efficiency. By applying multi-criteria decision making methods *Simple Additive Weighting* (SAW), *Multiplicative Exponential Weighting* (MEW) and *Complex Proportion Assessment* (COPRAS), the preferences of building owners regarding renovation measures were studied. The study highlighted four important criteria, including the use of energy from district heating and electricity, investment cost and payback period. The owner preferences were found to have a major impact on the outcome of the study. These owners gave sufficient weight to renovation measures within a short payback period. Renovation actions falling out to be quite attractive are additional thermal insulation in the attic and heat recovery from exhaust air.

Keywords: energy efficiency, rank, panel houses, renovation, SAW, MEW, COPRAS, AHP methods, MCDM.

# 1. Introduction

Industry is increasingly focusing on reducing its own energy consumption and CO<sub>2</sub> emissions with the aim of maximizing operational efficiency and reducing its overall carbon footprint (Ministry of Defence 2010). Clean Development Mechanism (CDM) has spurred the development of 4586 projects in 76 developing countries (Fennhan 2009). These projects are expected to reduce global greenhouse gas emissions up to 2.91 Gt CO<sub>2</sub>equivalent by 2012 (Boyd et al. 2009). Buildings have a significant and continuously increasing impact on the environment because they are responsible for a large portion of carbon emissions and the use of a considerable amount of resources and energy. The green building movement emerged to mitigate these effects and to improve the building construction process. This paradigm shift should bring significant environmental, economic, financial and social benefits (Castro-Lacouture et al. 2009). Protecting the natural environment is not the whole story: companies also must consider their social, economic and cultural impact (Werbach 2009).

In order to stop global warmth due to  $CO_2$  concentration, energy use should be decreased (Gao *et al.* 2001). Energy is an indispensable factor for the social and economic development of societies. The usage level of electricity is an indication of the economic prosperity of nations (Kahraman and Kaya 2010). Nowadays, an increase in carbon dioxide emissions contributes to an increase in surface temperature and is the primary cause for climatic changes. The basic measure that has been taken by the world community for the purpose of confrontation with this phenomenon was the use of Renewable Energy Sources (RES) (Economou 2010).

Energy consumption of buildings accounts for around 20-40% of all energy consumed in advanced countries. Over the last decade, more and more global organizations have been investing significant resources to create sustainably built environments, emphasizing sustainable building renovation processes to reduce energy consumption and carbon dioxide emissions (Juan et al. 2010). The construction sector covers one eighth of the total economic activity in the European Union (EU) employing more than eight million people. Intense activity in building construction, in conjunction with the need for energy savings and environmental protection policy, dictate for more reasonable design practices for buildings. The newly released EU Directive "Energy Performance of Buildings" (EPBD) concerns the use of energy in buildings and urges member nations of the EU to set stricter regulations regarding the efficient use of energy in buildings. For this reason, one of the main goals of advanced control systems, as applied to buildings, is to minimize energy consumption (Dounis and Caraiscos 2009). Building energy consumption keeps rising in recent years due to growth in population, increasing demand for healthy, comfortable and productive indoor environment, global climate changing, etc. Most of

energy use in buildings is for the provision of heating, ventilation and air conditioning (HVAC). High-level performance of HVAC systems in building lifecycle is critical to building sustainability (Xiao and Wang 2009).

#### 2. Project Description and Data for the Study

In the present study, multicriteria decision making methods will be applied to data on the effects and investment cost for a number of renovation measures aimed at improving energy efficiency. The data used are results from former work done by Bengt Bergqvist, Fredrik Gränne och Joel Kronheffer at Nordic Construction Company (NCC) in Sweden in co-operation with SonjaWidén, Ingela Blomberg and Marina Botta, KTH (Bergqvist *et al.* 2009).

The aim of the undertaken work was to assist in explaining the measures for energy saving that might show up to be profitable when apartment buildings produced in the period 1950 to 1970 have been to be renovated. By using multicriteria analysis, we will show how these results can be combined with the preferences of a group of building users and thus give guidance on how to make choices between renovation methods in a systematic and enlightened way.

## 2.1. Investigation Methodology

Building performance can be expressed employing different indicators such as primary energy use, environmental load and/or indoor environmental quality; building performance simulation can provide the decision maker with a quantitative measure of the extent to which an integrated design solution satisfies the design objectives and criteria (Heiselberg *et al.* 2009). Multi-criteria decision analysis (MCDA) methods have become increasingly popular in decision-making for sustainable energy because of the multi-dimensionality of the sustainability goal and the complexity of socio-economic and biophysical systems (Wang *et al.* 2009). There are a number of authors who use MCDA methods for the best alternative selection in different areas:

- Munier (2006) presented a multi-criteria method for treating difficult environmental problems where several alternatives or options are to be gauged through many different types of criteria;
- Tupenaite *et al.* (2010) describes the concept of the integrated analysis of built and human environment renovation as a whole as well as presents the multiple criteria assessment of alternatives for Bulgarian cultural heritage renovation projects. For this purpose, the widely known multiple criteria assessment methods SAW, TOPSIS and COPRAS and the newly developed method ARAS were used. As a result, the best project for granting was selected;
- Chen *et al.* (2006) presented a multi-criteria decision-making model for lifespan energy efficiency assessment of intelligent buildings (IBs). The decision-making model called IBAssessor is developed using an analytic network process (ANP)

method and a set of lifespan performance indicators for IBs selected applying a new quantitative approach called energy–time consumption index (ETI);

- Zavadskas *et al.* (2009b) presents the comparative analysis of dwelling maintenance contractors aimed at determining the degree of their utility for users and a bidding price of services by applying the method of multi-criteria complex proportional assessment (COPRAS);
- ALwaer and Clements-Croome (2010) use a consensus-based model (Sustainable Built Environment Tool – SuBETool) analysed going through the analytical hierarchical process (AHP) for multi-criteria decision-making;
- Juan *et al.* (2010) developed an integrated decision support system for office building renovation that not only assesses the current condition but also provides decision makers with solutions to sustainable renovation implementation;
- Kowalski *et al.* (2009) analyzed the combined use of scenario building and participatory multicriteria analysis (PMCA) in the context of renewable energy from a methodological point of view;
- In order to help decision-makers with the selection of the right materials, Castro-Lacouture *et al.* (2009) proposed a mixed integer optimization model incorporating design and budget constraints while maximizing the number of credits reached under the Leadership in Energy and Environmental Design (LEED) rating system.

To deal with this task, the authors use three multicriteria decision making methods:

- Simple Additive Weighting (SAW) method (Mac-Crimon 1968; Ginevičius et al. 2008a, b);
- Multiplicative Exponential Weighting (MEW) method (Zavadskas 1987);
- *COmplex PRoportion Assessment* (COPRAS) method (Zavadskas *et al.* 2008, 2009a).

For SAW and MEW methods as well as and for alternative " $\vec{i}$ ", the normalized  $\overline{x}_{ij}$  values of criterion "j" are calculated as follows:

$$\overline{x}_{ij} = \frac{x_{ij}}{\max_{i} x_{ij}}$$
 if maximum is preferable (1)

and  $x_{ij} \ge 0$ , under conditions  $x_{ij} \ge 0$ .

$$\overline{x}_{ij} = \frac{\min_{i} x_{ij}}{x_{ij}}$$
 if minimum is preferable (2)

and  $x_{ij} \ge 0$ , under conditions  $x_{ij} \ge 0$ .

$$\overline{x}_{ij} = \frac{\max_{i} x_{ij}}{x_{ij}} \quad \text{if maximum is preferable}$$
(3)

and  $x_{ij} < 0$ , under conditions  $x_{ij} < 0$ .

$$\overline{x}_{ij} = \frac{x_{ij}}{\min_{i} x_{ij}}$$
 if minimum is preferable (4)

and  $x_{ij} < 0$ , under conditions  $x_{ij} < 0$ .

There may be positive and negative values in one criterion column of the decision making matrix. In these cases, we recommend calculations using these formulas:

$$\overline{x}_{ij} = \frac{\min_{i} x_{ij}}{-(x_{ij}) + 2\min_{i} x_{ij}}$$
 if minimum is preferable (5)

and  $x_{ij} \ge 0$ , under conditions  $-\infty \le x_{ij} \le \infty$ .

$$\overline{x}_{ij} = \frac{x_{ij}}{\min x_{ij}}$$
 if minimum is preferableand  $x_{ij} < 0$ , (6)

under conditions  $-\infty \leq x_{ij} \leq \infty$ .

When applying COPRAS method, the normalized  $\bar{x}_{ij}$  values of *j* criterion for *i* alternative are calculated as follows:

$$\overline{x}_{ij} = \frac{x_{ij}}{\sum_{i=1}^{m} x_{ij}}$$
 if minimum is preferable or maximum  
$$\sum_{i=1}^{m} x_{ij}$$
 (7)

and  $x_{ij} < 0$ , under conditions  $x_{ij} < 0$ , or  $x_{ij} \ge 0$ , under conditions  $x_{ij} \ge 0$ .

For the solution where  $x_{ij} < 0$ ,  $\forall -\infty \le x_{ij} \le \infty$ , all values were transformed to positive values, and the vector of these numbers was taken as a value (distance from the lowest to the given value).

When applying the SAW method, optimality criterion  $L_i$  equals to the sum of the weighted criteria values:

$$L_i = \sum_{j=1}^n \left( \overline{x}_{ij} q_j \right). \tag{8}$$

When applying the MEW method, optimality criterion  $L_i$  equals to the multiplication of the weighted criteria values:

$$L_i = \prod_{j=1}^n \overline{x}_{ij}^{q_j},\tag{9}$$

where  $q_j$  is the weight of *j* criterion.

When applying the COPRAS method, optimality criterion  $Q_i$  is determined as follows:

$$Q_{i} = \frac{S_{+i} + \left(\min_{i} S_{i} \cdot \sum_{i=1}^{m} S_{-i}\right)}{S_{-i} \cdot \left(\sum_{i=1}^{m} \min_{i} S_{-i} / S_{-i}\right)}.$$
(10)

The weights of each criterion were determined using the AHP method (Saaty and Erdener 1979).

#### 2.2. Weights for Criteria Applying the AHP-Method

Multi-criteria decision methods need weights that in our case were determined applying the AHP-method (Saaty and Erdener 1979; Podvezko 2009). AHP stands for "Analytical Hierarchy Process". This method provides a proven effective means to deal with complicated decision

making. It is useful when identifying and weighting selection criteria, analyzing the data collected and expediting the decision making process.

The essence of the method is to construct a matrix expressing the relative values of a set of criteria. The method contains four steps (Medineckiene *et al.* 2010):

- a) to decompose the goal into its constituent parts and to develop a hierarchy of interrelated decision elements describing the problem;
- b) to make pair-wise comparisons with decision elements using a 9-point weighting scale to generate input data;
- c) to calculate the relative weights of the criteria relevant to the problem, which is technically called the Eigenvector;
- d) to aggregate the relative weights of decision elements to calculate ratings for alternative decision possibilities. The consistency ratio (CR) is calculated to check the opinions given as the basis for consistent decisions. A CR>0.1 indicates arbitrary judgments.

Table 1 shows the results of one of the interviewed owners. Table 2 indicates the pair-wise comparison matrix of the group results of building owners.

Table 1. Pair-wise comparison matrix of one of the interviewed

		District heat, energy consumption, MWh	Electricity for the facility, MWh	Cost for renovation, SEK	Payback period, year	q		
		$x_1$	<i>x</i> <sub>2</sub>	<i>x</i> <sub>3</sub>	$x_4$			
District heat, energy consumption, MWh	$x_1$	1	1.00	3.00	1/5	0.162		
Electricity for the facility, MWh	<i>x</i> <sub>2</sub>	1	1	3.00	1/5	0.162		
Cost for renovation, SEK	<i>x</i> <sub>3</sub>	1/3	1/3	1	1/5	0.075		
Payback period, year	<i>x</i> <sub>4</sub>	5	5	5	1	0.601		
CR = 0.06								

Table 2. Pair-wise comparison matrix of the group results

District heat, energy consumption, MWh	Electricity for the facility, MWh	Cost for renovation, SEK	Payback period, year	q
<i>x</i> <sub>1</sub>	<i>x</i> <sub>2</sub>	<i>x</i> <sub>3</sub>	<i>x</i> <sub>4</sub>	
District heat, energy consumption, MWh $x_1$ 1.00	0.447	0.656	0.209	0.06
Electricity for the facility, MWh $x_2$ 2.24	1.00	1.00	0.611	0.23
$\begin{array}{c c} \text{Cost for renovation,} \\ \text{SEK} \end{array}  x_3  1.52 \end{array}$	1.00	1.00	0.352	0.24
Payback period, year $x_4$ 4.78	1.64	2.84	1.00	0.47
CR = 0	0.01			

The choices in this study were based on the opinions given by persons having attitudes typical to facility owners. All the weights of each criterion were determined applying the AHP method. There was a pair-wise comparing matrix produced to show the owner's possible decisions. In this matrix, the criteria to be compared were the use of energy for district heating and electricity, investment cost and a payback period respectively.

# 2.3. Case Study

Three apartment buildings in Swedish residential areas built in '50s, '60s and '70s were selected. Each of these buildings included calculations on the effects and investment cost of a number of renovation measures aimed at improving energy efficiency. All actions on renovation were evaluated with regard to the use of energy from district heating and electricity respectively, investment cost and payback time. Energy calculations were done considering E-norm, which is energy calculation software commonly used in Sweden. In the base case, which is reference to each of the buildings, calculations are done using in-data like when the building was new. Costs were calculated based on data about experiences from NCC. Table 3 presents the properties of importance for the buildings discussed in the study.

In calculations on the base case, the following input data is used:

- Room temperature in the apartments is set to +22 °C and in stair houses - to +20 °C;

- The air tightness of the building envelope is described with a leakage flow of 2.0 l/s, m<sup>2</sup> in the surrounding area at 50 Pa of pressure difference. Calculations indicate that air flow through the building envelope is constantly 5% of this value. This is calculated on the entire surrounding area of the building;
- Incoming solar radiation through the windows is calculated by assuming a mean sun shading factor of 0.5. This means that the gain of solar energy is 50% of the gain possible through a 2-pane window with no solar shading;
- Annual energy consumption for hot tap water is reckoned to be 25 kWh/m<sup>2</sup> A<sub>temp</sub>, *a*;
- The consumption of household electricity is set to be 30 kWh/m<sup>2</sup> A<sub>temp</sub>, *a*;
- The flow of supply air per year is set to be 0.35 *l*/s, m<sup>2</sup> A<sub>temp</sub>;
- The inhabitants airing of their apartments are supposed to result in an additional need for heating of 4 kWh/m<sup>2</sup>, a.

It should be kept in mind that when a number of measures for renovation are combined into a package, compound savings are usually lower than the sum of the savings from the measures one by one.

The initial matrix describing the problem is presented in Table 4.

The number of the building (marking)	B1	B2	В3
Name of the building	Svärdsidan 1, Östberga Built in 1967–1969.	Förvaltarvägen 4 Built in 1952–1953.	BRF Toppsockret Hökarängen Built in 1964.
Short descrip- tion	24 apartments in each building Four storeys and a basement (three houses sharing a substation for district heating).	28 apartments in one of five point blocks. Seven storeys and a base- ment (three houses sharing a substa- tion for district heating).	143 apartments in 17 stairways Four to five storeys (three houses sharing a substa- tion for district heating).
Heated area	The whole area $A_{temp} = 3219 \text{ m}^2$ , apartments of which cover 2485 m <sup>2</sup> and a subsidiary usable area 734 m <sup>2</sup> .	The whole area $A_{temp} = 2184 \text{ m}^2$ , apartments of which cover 1797 m <sup>2</sup> and a subsidiary usable area 387 m <sup>2</sup> .	The whole area $A_{temp} =$ 14 700 m <sup>2</sup> , apartments of which cover 10900 m <sup>2</sup> and a subsidi- ary usable area 3800 m <sup>2</sup> .
Description of building con- struction	Wall construction: 15 cm concrete +15 cm lightweight concrete with rendering; U-value is about 0.75 W/m <sup>2</sup> ,K. Dual-pane window, U-value is about 2.7 W/m <sup>2</sup> ,K in the stair-case, Single-pane window; U-value is about 5 W/m <sup>2</sup> ,K in the gateway.	Wall construction: 25 cm light- weight concrete with rendering; U-value is about 0.7 W/m <sup>2</sup> ,K. The attic was originally insulated with 5 cm coke and cinder with the U-value of 0.6 W/m <sup>2</sup> ,K.	Wall construction: 25 cm light- weight concrete with rendering, U-value about is 0.7 W/m <sup>2</sup> ,K. Three glass windows, U-value is about 2.0 W/m <sup>2</sup> ,K. Glazed balconies.
Building ser- vices	Substation for district heating serving three houses. Balanced ventilation with supply air and exhaust air driven by electrical ventilators.	Substation for district heating serving in one of the buildings. Exhaust air ventilation driven by electrical ventilators.	Substation for district heating serving in one of the buildings. Exhaust air ventilation driven by electrical ventilators with air intake through gap air ventila- tors in the window frames.

Table 3. Description of buildings

Table 4.	The	initial	matrix	describing	the	problem

$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	Tuble	• • • • • • •				•	
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	Alternative number	Building number	Description of the actions	District heat, energy consump- tion, MWh	Electricity for the facility, MWh	Cost for renova- tion, SEK	Payback period, year
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	1		Thermal insulation added in the attic. Additional insulation is 300 mm	-17.40	-0.04	90 000	
33         insulation will be 0.2 Wm <sup>2</sup> , K. Cost will reach 300 STK/m <sup>2</sup> .         -229.10         -0.72         1215.000         7.           4         B1         Thermal insulation addet to facales. The example covers 150 mm of         -78.80         -0.02         14700 000         28           6         B3         ing envelope has been improved from 2.0 to 1.5 <i>l</i> 's,m <sup>2</sup> at a surrounding         -79.80         -0.02         1700 000         28           7         B1         New windows and doors have         -80.50         -0.20         1600 000         25           8         B2         1.0 Wm <sup>2</sup> , K. Insultation strong from 4.0 to         -95.70         -0.20         1625 000         22           9         B3         2.0 Wm <sup>2</sup> , K. Insultation strong from 2.0 to 1.0 <i>l</i> 's,m <sup>2</sup> at 50 Pa         -95.70         -0.20         1625 000         22           9         B3         2.0 Wm <sup>2</sup> , K. In tightness of the building envelope has been improve         -45.80         -0.00         70         162         162         162         50         -0.20         1625 000         22           10         B1         tightness of the building envelope has been improve         -45.30         -0.00         70         to 50         57         -0.20         1625 000         20         162         163							
	4		Thermal insulation added to facades. The example covers 150 mm of				39
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	5	B2		-79.80	-0.02	1 750 000	28
Ing introduct non-construction in protect non-constructin the proteconstructin protect non-construction in protect non							
been assumed to improve the U-value of windows from 2.7 to $-95.70$ $-0.20$ $1625 000$ $22$ 9B3 $2.0 Wm^2 K$ . The tightness of the building envelope has been improved from 2.0 till $1.0 Wm^2 K$ and that of the gateway parts of the building from 2.0 till $1.0 Wm^2 K$ . The tightness of the building from 2.0 to $1.0 Vm^2 K$ . The tightness of the building from 2.0 to $1.0 Vm^2 K$ . The tightness of the building from 2.0 to $1.0 Vm^2 K$ . The tightness of the building from 2.0 to $1.0 Vm^2 K$ . The tightness of the building from 2.0 to $1.0 Vm^2 K$ . The tightness of the building from 2.0 to $1.0 Vm^2 K$ . The tightness of the building from 2.0 to $1.0 Vm^2 K$ . The tightness of the building from 2.0 to $1.0 Vm^2 K$ . The tightness of the windows is assumed to improve the tightness of the windows from 2.0 to $1.0 Vm^2 K$ . The tightness of the windows is assumed to improve the tightness of the windows from 2.0 to $1.0 Vm^2 K$ . The tightness of the windows is assumed to improve the tightness of the windows is assumed to improve the tightness of the windows is assumed to improve the tightness of the windows is assumed to improve the tightness of the windows is assumed to improve the tightness of the windows is assumed to improve the tightness of the windows is assumed to improve the tightness of the windows is assumed to improve the tightness of the windows is assumed to improve the tightness of the window is assumed to improve the tightness of the window is assumed to improve the tightness of the window is assumed to improve the tightness of the window is assumed to improve the tightness of the window is assumed to improve the tightness of the window is assumed to improve the tightness of the window is assumed to improve the tightness assumed to improve tight the window is assumed to improve the tight tightness window is assumed to improve the tight tightness assumed to improve the tight tightness and the assume trans the tradio device the tis	0	В3	area of 50 Pa.				
8         B2         1.0 W/m <sup>2</sup> K and that of the gateway parts of the buildings from 4.0 to from 2.0 till 1.0 l/s.m <sup>2</sup> at 50 Pa of pressure difference.         -95.70         -0.20         1 625.000         22           9         B3         2.0 W/m <sup>2</sup> K. In the tightness of the building strong windows is assumed to improve from 2.0 till 1.0 l/s.m <sup>2</sup> at 50 Pa of pressure         -453.80         -1.70         9.900.000         27           10         B1         Tightening around windows. Tightening windows is assumed to improve the tightness of the windows from 2.0 to 1.0 ks.m <sup>2</sup> at 50 Pa of pressure         -14.10         0.00         82 000         7           11         B2         B3         difference. Cost - 500 SEK/window.         -64.60         10.50         650 000         17           14         B2         robust assess of installing such assess of installing such assess of installing such system that is supposed to give the efficiency of 60%.         -64.60         10.50         6000 00         11           17         B2         exchangers is supposed to give the efficiency of 80%.         -548.00         -85.60         10.50         600000         5           19         B1         Heat recovery using a heat pump taking heat from exhaust air is ultical and frequipment can give a COP         -548.00         63.80         1800000         5           19         B1         Heat recovery using a hea	7						
	8	B2	1.0 W/m <sup>2</sup> ,K and that of the gateway parts of the buildings from 4.0 to	-95.70	-0.20	1 625 000	22
	9	В3	2.0 W/m <sup>2</sup> ,K. The tightness of the building envelope has been improved from 2.0 till 1.0 $l/s$ ,m <sup>2</sup> at 50 Pa of pressure difference.	-453.80	-1.70	9 900 000	27
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	10		Tightening around windows. Tightening windows is assumed to improve				
	11	B2		-19.30	0.00	70 500	5
14B2 to living rooms and a sleeping room can be supplied with a low risk of problems with draught, because heat from exhaust air is utilized. A drawback is relatively high expenses of installing such system that is supposed to give the efficiency of 60%76.705.30350 000816B1Heat recovery from ventilation air, using regenerative heat exchangers is supposed to give the efficiency of 60%406.3070.301 800 000917B2 with 80% efficiency. The installation of a system with regenerative heat exchangers is supposed to give the efficiency of 80%86.6010.50600 0001117B2 with 80% efficiency. The installation of a system with regenerative heat exchangers is supposed to give the efficiency of 80%86.6010.50600 0002820B2 buildings with not very high costs. This kind of equipment can give a COP means the ratio between the heat produced and the amount of electric energy consumed for driving a compressor and pumps for circulation71.60-0.2042.0002221B3Adjustment of a heating system and valves in thermostats. Cost for ad- about 1500 SEK per apartment73.80-0.2042.000222B1Adjustment of a heating system is supposed to give a savings because the aver- age temperature in the building can go down with 1°C. Cost may be at about 1500 SEK per apartment73.60-0.00112 00001124B3about 4000 SEK per apartment73.60-0.00120.001125B1Installation of an othe sof systems for temperature about 000 SEK per apartment.	12	B3	difference. Cost – 500 SEK/window.	-85.70	-0.20	357 000	5
14H216 living rooms and a sleeping room can be supplied with a low risk of problems with draught, because heat from exhaust air is utilized. A drawback is relatively high expenses of installing such system that is supposed to give the efficiency of 60%76.705.30350 000816B1Heat recovery from ventilation air, using regenerative heat exchangers with 80% efficiency. The installation of a system with regenerative heat exchangers is supposed to give the efficiency of 80%86.6010.50600 0001117B2exchangers is supposed to give the efficiency of 80%548.0069.801 800 000519B1Heat recovery using a heat pump taking heat from exhaust air. A heat pump taking heat from exhaust air can often be installed in apartment buildings with not very high costs. This kind of equipment can give a COP energy consumed for driving a compressor and pumps for circulation165.7065.601 450 0002320B2buildings with not very high costs. This kind of equipment can give a COP energy consumed for driving a compressor and pumps for circulation27.60-0.2042 000221B3Adjustment of a heating system and valves in thermostats. Cost for ad- abut 1500 SEK per apartment118.60-1.40215 000222B1Adjustment of a heating system is supposed to give savings in the realmity vidual metering for hot tap water is supposed to give savings in the realmity vidual metering for hot tap water. Indi- vidual metering for hot tap water. Supposed to give savings in the realmity-27.60-0.20112 00025B1Insta	13	B1					
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	14	B2		-76.70	5.30	350 000	8
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	15	В3	problems with draught, because heat from exhaust air is utilized. A drawback is relatively high expenses of installing such system that is	-406.30	70.30	1 800 000	9
17B2exchangers is supposed to give the efficiency of 80%. $-102.30$ $3.30$ $330000$ $3$ 18B3Heat recovery using a heat pump taking heat from exhaust air. A heat pump taking heat from exhaust air can often be installed in apartment buildings with not very high costs. This kind of equipment can give a COP means the ratio between the heat produced and the amount of electric energy consumed for driving a compressor and pumps for circulation. $-165.70$ $65.60$ $1500000$ $23$ 22B1Adjustment of a heating system is supposed to give savings because the aver- age temperature in the building can go down with 1 °C. Cost may be at of 20%, which means 20–25 KWh/m². The cost of notat about 1500 SEK per apartment. $-27.60$ $-0.20$ $42.000$ $2$ 24B3 about 1500 SEK per apartment. $-118.800$ $-1.40$ $215000$ $2$ 25B1Installation of equipment for individual metering for hot tap water. Indi- vidual metering for hot tap water is supposed to give savings in the realm of 20%, which means 20–25 KWh/m². The cost of installation estimates $-9.90$ $0.00$ $96000$ $12$ 27B3about 4000 SEK, per apartment while the cost of the meter makes about $400$ SEK. Cost for reading meters is not included. $-73.50$ $0.00$ $572.000$ $10$ 38B1Installation of solar collector is about 500 SEK per may thich also in- recase in the indoor temperature of 1 °C. Cost may reach about 4000 $572.000$ $14.70$ $786.500$ $12$ 33B3B3collectors are supposed to give a general de- crease in the indoor temperature of 1 °C. Cost m	16	B1		-86.60	10.50	600 000	11
18B3exchangers is supposed to give the efficiency of 80%548.0069.801 800 000519B1Heat recovery using a heat pump taking heat from exhaust air. A heat pump taking heat from exhaust air can often be installed in apartment buildings with not very high costs. This kind of equipment can give a COP (coefficient of performance) of 2.5 reckoned as annual efficiency. COP means the ratio between the heat produced and the amount of electric energy consumed for driving a compressor and pumps for circulation0165.7065.601 500 0002321B3(coefficient of performance) of 2.5 reckoned as annual efficiency. COP means the ratio between the heat produced and the amount of electric energy consumed for driving a compressor and pumps for circulation01.04446.207 150 0002322B1Adjustment of a heating system and valves in thermostats. Cost for ad- about 1500 SEK per apartment27.60-0.2042 000224B3 age temperature in the building can go down with 1°C. Cost may be at about 1500 SEK per apartment12.400.00112 0001126B202%, which means 20-25 KM/m². The cost of installation estimates 4000 SEK. Cost for reading meters is not included9.900.0096 0001228B1Installation of individual metering for hot tap water73.500.00572 0001028B1Installation of solar collector is shout 500 SEK per afartment13.860-1.40572 000531B1Installation of solar collectors for hot tap water.Arule of thum bis that a so	17	B2		-102.30	5.30	350 000	5
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$			exchangers is supposed to give the efficiency of 80%.				
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$			Heat recovery using a heat nump taking heat from exhaust air. A heat				
20B2buildings with not very high costs. This kind of equipment can give a COP (coefficient of performance) of 2.5 reckoned as annual efficiency. COP means the ratio between the heat produced and the amount of electric energy consumed for driving a compressor and pumps for circulation. $-1169.40$ $446.20$ $7150\ 000$ $18$ 22B1Adjustment of a heating system and valves in thermostats. Cost for ad- about 1500 SEK per apartment. $-27.60$ $-0.20$ $42\ 000\ 2$ 24B3age temperature in the building can go down with 1 °C. Cost may be at about 1500 SEK per apartment. $-138.60\ -1.40\ 215\ 000\ 2$ 25B1Installation of equipment for individual metering for hot tap water. Indi- vidual metering for hot tap water is supposed to give savings in the realm of 20%, which means $20-25\ KWhm^2$ . The cost of installation estimates about 4000 SEK. Cost for reading meters is not included. $-12.40\ 0.00\ 112\ 000\ 112\ -73.50\ 0.00\ 572\ 000\ 10\ -73.50\ 0.00\ 572\ 000\ 10\ -73.50\ 0.00\ 572\ 000\ 10\ -33.80\ -0.20\ 96\ 000\ 4\ -33$							
21B3(coefficient of performance) of 2.5 reckoned as annual efficiency. COP means the ratio between the heat produced and the amount of electric energy consumed for driving a compressor and pumps for circulation. $-1169.40$ $446.20$ $7150\ 000$ $18$ 22B1Adjustment of a heating system and valves in thermostats. Cost for ad- justing the heating system is supposed to give savings because the aver- about $1500\ SEK$ per apartment. $-27.60$ $-0.20$ $42\ 000$ $2$ 24B3age temperature in the building can go down with $1^\circ$ C. Cost may be at about $1500\ SEK$ per apartment. $-138.60$ $-1.40$ $215\ 000$ $2$ 25B1Installation of equipment for individual metering for hot tap water. Indi- vidual metering for hot tap water is supposed to give savings in the realm of $20\%$ , which means $20-25\ KWh/m^2$ . The cost of installation cests of installation estimates about $4000\ SEK$ . Cost for reading meters is not included. $-9.90$ $0.00$ $96\ 000$ $12$ 28B1Installation of individual metering for hot tap water. Indi- with all nuch higher than those of systems for temperature metering. Individual energy metering is supposed to give a general de- crease in the indoor temperature of $1\ ^\circ$ C. Cost may reach about $4000\$ SEK per apartment. $-15.30\$ $2.20\$ $154\ 000\$ $4$ 31B1Installation of solar collectors for hot tap water. A rule of thumb is that a solar collectors are supposed to be installed on the roofs of the building and to cover an area of about $3\ ^\circ$ for each apartment. An accumulator tank for heat storage will be installed in the basement. $-15.30\$ $2.20\$ $132\ 000\$	20	B2		-201.90	80.60	1 450 000	23
22B1Adjustment of a heating system and valves in thermostats. Cost for adjusting the heating system is supposed to give savings because the averabout 1500 SEK per apartment. $-27.60$ $-0.20$ $42000$ $2$ 24B3age temperature in the building can go down with 1 °C. Cost may be at about 1500 SEK per apartment. $-138.60$ $-1.40$ $215000$ $2$ 25B1Installation of equipment for individual metering for hot tap water is supposed to give savings in the realm of 20%, which means 20–25 KWh/m². The cost of installation estimates about 4000 SEK. Cost for reading meters is no included. $-12.40$ $0.00$ $112000$ $11$ 26B2of 20%, which means 20–25 KWh/m². The cost of installation estimates about 4000 SEK. Cost for reading meters is no included. $-9.90$ $0.00$ $96000$ $12$ 28B1Installation of individual metering for heat. Installation costs of energy metering. Individual metering is supposed to give a general decrease in the indoor temperature of 1 °C. Cost may reach about 4000 $-73.50$ $0.00$ $572000$ $5$ 30B3Installation of solar collectors for hot tap water. A rule of thumb is that a clueds a control unit and a pump for circulation and accumulator tank. Solar collectors are supposed to be installed on the roofs of the buildings and to cover an area of about $3 m^2$ for each apartment. An accumulator tank for heat storage will be installed in the basement. $-15.30$ $0.20$ $14.70$ $786500$ $12$ 34B1Installation of water taps giving lower water flow than usual. By using energy effective water taps, it is possible to save $20-40\%$ of hot tap water. $-13.90$ $0.00$ $1$	21	B3	(coefficient of performance) of 2.5 reckoned as annual efficiency. COP means the ratio between the heat produced and the amount of electric	-1 169.40	446.20	7 150 000	18
23B2justing the heating system is supposed to give savings because the average temperature in the building can go down with 1 °C. Cost may be at about 1500 SEK per apartment. $-33.80$ $-0.20$ $36000$ $2$ 24B3about 1500 SEK per apartment. $-138.60$ $-1.40$ $215000$ $2$ 25B1Installation of equipment for individual metering for hot tap water. Individual metering for hot tap water is supposed to give savings in the realm of 20%, which means $20-25$ KWh/m <sup>2</sup> . The cost of installation estimates about $400$ SEK, cost for reading meters is not included. $-12.40$ $0.00$ $112000$ $11$ 26B2of 20%, which means $20-25$ KWh/m <sup>2</sup> . The cost of installation estimates about $400$ SEK, Cost for reading meters is not included. $-9.90$ $0.00$ $96000$ $12$ 27B3about 4000 SEK, Cost for reading meters is not included. $-73.50$ $0.00$ $572000$ $10$ 28B1Installation of individual metering for heat. Installation costs of energy metering. Individual emerger metering is supposed to give a general decrease in the indoor temperature of 1 °C. Cost may reach about 4000 $-138.60$ $-1.40$ $572000$ $5$ 31B1Installation of solar collectors for hot tap water. A rule of thumb is that a solar collector can produce $200-400$ KWh/m <sup>2</sup> per year for hot tap water. $-15.30$ $2.20$ $154000$ $16$ 33B3Cludes a control unit and a pump for circulation and accumulator tank. Solar collectors are supposed to be installed on the roofs of the buildings and to cover an area of about 3 m <sup>2</sup> for each apartment. An accumulator tank for heat storage will be installed i	22	B1		-27.60	-0.20	42 000	2
24B3 about 1500 SEK per apartment.age temperature in the building can go down with 1 °C. Cost may be at about 1500 SEK per apartment. $-138.60$ $-1.40$ $215\ 000$ 225B1Installation of equipment for individual metering for hot tap water. Individual metering for hot tap water is supposed to give savings in the realm of 20%, which means 20–25 KWh/m². The cost of installation estimates about 4000 SEK per apartment while the cost of the meter makes about 400 SEK. Cost for reading meters is not included. $-12.40$ $0.00$ $112\ 000$ $11$ 28B1Installation of individual metering for heat. Installation costs of energy metering will be much higher than those of systems for temperature metering. Individual energy metering is supposed to give a general de- crease in the indoor temperature of 1 °C. Cost may reach about 4000 SEK per apartment. $-27.60$ $-0.20$ $112\ 000$ $5$ 31B1Installation of solar collectors for hot tap water. A rule of thumb is that a solar collector can produce 200–400 KWh/m² per year for hot tap water. The cost of a solar collector is about 5000 SEK per m², which also in- cludes a control unit and a pump for circulation and accumulator tank for heat storage will be installed on the roofs of the buildings and to cover an area of about 3 m² for each apartment. An accumulator tank for heat storage will be installed in the basement. $-15.30$ $0.00$ $227\ 000$ $19$ 34B1Installation of water taps, it is possible to save $20-40\%$ of hot tap water and the same amount of cold tap water. $-13.90\ 0.00\ 195\ 000\ 195\ 000\ 195\ 000\ 195\ 000\ 195\ 000\ 195\ 000\ 195\ 000\ 195\ 000\ 195\ 000\ 195\ 000\ 195\ 000\ 195\ 000\ 195\ 000\ 195\ 000\ 195\ $							
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$26$ B2of 20%, which means 20–25 KWh/m². The cost of installation estimates about 4000 SEK per apartment while the cost of the meter makes about 400 SEK. Cost for reading meters is not included. $-9.90$ $0.00$ $96\ 000$ $12$ $27$ B3about 4000 SEK per apartment while the cost of the meter makes about 400 SEK. Cost for reading meters is not included. $-73.50$ $0.00$ $572\ 000$ $10$ $28$ B1Installation of individual metering for heat. Installation costs of energy metering. Individual energy metering is supposed to give a general de- crease in the indoor temperature of 1 °C. Cost may reach about 4000 SEK per apartment. $-27.60$ $-0.20$ $112\ 000$ $5$ $31$ B1Installation of solar collectors for hot tap water. A rule of thumb is that a solar collector can produce 200–400 KWh/m² per year for hot tap water. $-15.30$ $2.20$ $154\ 000$ $16$ $32$ B2solar collector can produce 200–400 KWh/m² per year for hot tap water. The cost of a solar collector is about 5000 SEK per m², which also in- cludes a control unit and a pump for circulation and accumulator tank. Solar collectors are supposed to be installed on the roofs of the buildings and to cover an area of about 3 m² for each apartment. An accumulator tank for heat storage will be installed in the basement. $-15.30$ $0.00$ $227\ 000$ $19$ $34$ B1Installation of water taps, it is possible to save 20–40% of hot tap water. $-13.90$ $0.00$ $195\ 000$ $18$	25	B1	Installation of equipment for individual metering for hot tap water. Indi-	-12.40	0.00	112 000	11
$400$ SEK. Cost for reading meters is not included. $-27.60$ $-0.20$ $112\ 000$ $5$ $29$ B2metering will be much higher than those of systems for temperature metering. Individual energy metering is supposed to give a general de- crease in the indoor temperature of 1 °C. Cost may reach about 4000 SEK per apartment. $-33.80$ $-0.20$ $96\ 000$ $4$ $31$ B1Installation of solar collectors for hot tap water. A rule of thumb is that a solar collector can produce $200-400$ KWh/m² per year for hot tap water. $-15.30$ $2.20$ $154\ 000$ $16$ $32$ B2Solar collector can produce $200-400$ KWh/m² per year for hot tap water. The cost of a solar collector is about $5000$ SEK per m², which also in- cludes a control unit and a pump for circulation and accumulator tank. Solar collectors are supposed to be installed on the roofs of the buildings and to cover an area of about $3\ m^2$ for each apartment. $-15.30\ 0.00\ 227\ 000\ 19$ $34$ B1Installation of water taps giving lower water flow than usual. By using energy effective water taps, it is possible to save $20-40\%$ of hot tap water $-13.90\ 0.00\ 195\ 000\ 18$ $35$ B2	26	B2		-9.90	0.00	96 000	12
28B1Installation of individual metering for heat. Installation costs of energy metering will be much higher than those of systems for temperature metering. Individual energy metering is supposed to give a general de- crease in the indoor temperature of 1 °C. Cost may reach about 4000 $-27.60$ $-0.20$ $112\ 000$ $5$ 30B3crease in the indoor temperature of 1 °C. Cost may reach about 4000SEK per apartment. $-138.60$ $-1.40$ $572\ 000$ $5$ 31B1Installation of solar collectors for hot tap water.A rule of thumb is that a solar collector can produce $200-400\ KWh/m^2$ per year for hot tap water. $-15.30$ $2.20$ $154\ 000$ $16$ 33B3collector san produce $200-400\ KWh/m^2$ per year for hot tap water. $-102.90$ $14.70$ $786\ 500$ $12$ 34B1Installation of water taps giving lower water flow than usual. By using energy effective water taps, it is possible to save $20-40\%$ of hot tap water $-15.30$ $0.00$ $227\ 000$ $19$ 35B2and the same amount of cold tap water. $-13.90$ $0.00$ $195\ 000$ $18$	27	B3		-73.50	0.00	572 000	10
29B2metering will be much higher than those of systems for temperature metering. Individual energy metering is supposed to give a general de- crease in the indoor temperature of 1 °C. Cost may reach about 4000 SEK per apartment. $-33.80$ $-0.20$ $96000$ $4$ $31$ B1Installation of solar collectors for hot tap water. A rule of thumb is that a solar collector can produce 200–400 KWh/m² per year for hot tap water. The cost of a solar collector is about 5000 SEK per m², which also in- cludes a control unit and a pump for circulation and accumulator tank. Solar collectors are supposed to be installed on the roofs of the buildings and to cover an area of about 3 m² for each apartment. An accumulator tank for heat storage will be installed in the basement. $-15.30$ $2.20$ $14.70$ $786500$ $12$ $34$ B1Installation of water taps giving lower water flow than usual. By using energy effective water taps, it is possible to save 20–40% of hot tap water and the same amount of cold tap water. $-13.90$ $0.00$ $227000$ $19$ $-13.90$ $0.00$ $195000$ $18$	28	B1	Installation of individual metering for heat. Installation costs of energy	-27.60	-0.20	112 000	5
30B3metering. Individual energy metering is supposed to give a general decrease in the indoor temperature of 1 °C. Cost may reach about 4000 SEK per apartment. $-138.60$ $-1.40$ $572\ 000$ $5$ 31B1Installation of solar collectors for hot tap water. A rule of thumb is that a solar collector can produce 200–400 KWh/m² per year for hot tap water. The cost of a solar collector is about 5000 SEK per m², which also in- cludes a control unit and a pump for circulation and accumulator tank. Solar collectors are supposed to be installed on the roofs of the buildings and to cover an area of about 3 m² for each apartment. An accumulator tank for heat storage will be installed in the basement. $-15.30$ $2.20$ $132\ 000$ $15$ 34B1Installation of water taps giving lower water flow than usual. By using energy effective water taps, it is possible to save 20–40% of hot tap water and the same amount of cold tap water. $-13.90$ $0.00$ $227\ 000$ $19$ $-13.90$ $0.00$ $195\ 000$ $18$	29	B2	metering will be much higher than those of systems for temperature	-33.80	-0.20	96 000	4
31B1Installation of solar collectors for hot tap water. A rule of thumb is that a solar collector can produce 200–400 KWh/m² per year for hot tap water. The cost of a solar collector is about 5000 SEK per m², which also in- cludes a control unit and a pump for circulation and accumulator tank. Solar collectors are supposed to be installed on the roofs of the buildings and to cover an area of about 3 m² for each apartment. An accumulator tank for heat storage will be installed in the basement. $-15.30$ $2.20$ $154\ 000$ $16$ 34B1Installation of water taps giving lower water flow than usual. By using energy effective water taps, it is possible to save 20–40% of hot tap water and the same amount of cold tap water. $-15.30$ $2.20$ $154\ 000$ $16$ $-102.90$ $14.70$ $786\ 500$ $12$ $-102.90$ $14.70$ $786\ 500$ $12$ $-102.90$ $14.70$ $786\ 500$ $12$ $-102.90$ $14.70$ $786\ 500$ $12$ $-102.90$ $14.70$ $786\ 500$ $12$ $-102.90$ $14.70$ $786\ 500$ $12$ $-102.90$ $14.70$ $786\ 500$ $12$ $-102.90$ $14.70$ $786\ 500$ $12$ $-102.90$ $14.70$ $786\ 500$ $12$ $-102.90$ $14.70$ $786\ 500$ $12$ $-102.90$ $14.70$ $786\ 500$ $12$ $-13.90$ $0.00$ $227\ 000$ $19$ $-13.90$ $0.00$ $195\ 000$ $18$	30	В3	crease in the indoor temperature of 1 °C. Cost may reach about 4000	-138.60	-1.40	572 000	5
32B2solar collector can produce 200–400 KWh/m² per year for hot tap water. The cost of a solar collector is about 5000 SEK per m², which also in- cludes a control unit and a pump for circulation and accumulator tank. Solar collectors are supposed to be installed on the roofs of the buildings and to cover an area of about 3 m² for each apartment. An accumulator tank for heat storage will be installed in the basement. $-13.90$ $2.00$ $132\ 000$ $15$ 34B1Installation of water taps giving lower water flow than usual. By using energy effective water taps, it is possible to save 20–40% of hot tap water and the same amount of cold tap water. $-13.90$ $2.00$ $132\ 000$ $15$ $-102.90$ $14.70$ $786\ 500$ $12$ $-102.90$ $14.70$ $786\ 500$ $12$ $-102.90$ $-15.30$ $0.00$ $227\ 000$ $19$ $-13.90$ $0.00$ $195\ 000$ $18$	31	B1		-15.30	2.20	154 000	16
33B3The cost of a solar collector is about 5000 SEK per m², which also includes a control unit and a pump for circulation and accumulator tank. Solar collectors are supposed to be installed on the roofs of the buildings and to cover an area of about 3 m² for each apartment. An accumulator tank for heat storage will be installed in the basement102.9014.70786 5001234B1Installation of water taps giving lower water flow than usual. By using energy effective water taps, it is possible to save 20–40% of hot tap water and the same amount of cold tap water15.300.00227 00019-13.900.00195 00018		B2	solar collector can produce 200–400 KWh/m <sup>2</sup> per year for hot tap water.				
Solar collectors are supposed to be installed on the roofs of the buildings and to cover an area of about 3 m² for each apartment. An accumulator tank for heat storage will be installed in the basement15.300.00227 0001934B1Installation of water taps giving lower water flow than usual. By using energy effective water taps, it is possible to save 20–40% of hot tap water and the same amount of cold tap water15.300.00227 00019							
35B2energy effective water taps, it is possible to save 20–40% of hot tap water-13.900.00195 00018		105	Solar collectors are supposed to be installed on the roofs of the buildings and to cover an area of about 3 $m^2$ for each apartment. An accumulator tank for heat storage will be installed in the basement.	102.90	11.70	700 200	
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	34	B1		-15.30	0.00	227 000	19
	35	B2		-13.90	0.00	195 000	18
	36	B3		-102.90	0.00	1 158 000	14

## 3. Results and Discussion

Table 5 shows the initial decision making matrix of the described problem.

The names of the criteria can be defined in the following way:

- criterion x<sub>1</sub> is energy consumption of district heat, MWh;
- criterion  $x_2$  is electricity for the facility, MWh;
- criterion  $x_3$  is the total cost of renovation, SEK;
- criterion  $x_4$  is a payback period per year.

Table 5. The initial matrix of the described problem

Alterna-	$x_1$	<i>x</i> <sub>2</sub>	<i>x</i> <sub>3</sub>	<i>x</i> <sub>4</sub>
tive		Optimizat	ion direction	
	min	min	min	min
q	0.06	0.23	0.24	0.47
$A_1$	-17.40	-0.04	90 000.00	7.00
A2	-33.00	-0.08	150 000.00	6.00
	229.10	-0.75	1 215 000.00	7.00
$A_4$	-78.50	-0.20	2 450 000.00	39.00
$A_5$	-79.80	-0.02	1 750 000.00	28.00
$A_6$ -	202.30	-0.75	7 437 500.00	46.00
	-80.50	-0.20	1 600 000.00	25.00
$A_8$	-95.70	-0.20	1 625 000.00	22.00
$A_9$ -	453.80	-1.70	9 900 000.00	27.00
A <sub>10</sub>	-14.10	0.00	82 000.00	7.00
A <sub>11</sub>	-19.30	0.00	70 500.00	5.00
	-85.70	-0.20	357 000.00	5.00
	-64.60	10.50	650 000.00	17.00
	-76.70	5.30	350 000.00	8.00
	406.30	70.30	1 800 000.00	9.00
	-86.60	10.50	600 000.00	11.00
	102.30	5.30	350 000.00	5.00
	548.00	69.80	1 800 000.00	5.00
	165.70	65.60	1 500 000.00	28.00
	201.90	80.60	1 450 000.00	23.00
	169.40	446.20	7 150 000.00	18.00
	-27.60	-0.20	42 000.00	2.00
	-33.80	-0.20	36 000.00	2.00
	138.60	-1.40	215 000.00	2.00
	-12.40	0.00	112 000.00	11.00
$A_{26}$	-9.90	0.00	96 000.00	12.00
A <sub>27</sub>	-73.50	0.00	572 000.00	10.00
A <sub>28</sub>	-27.60	-0.20	112 000.00	5.00
A <sub>29</sub>	-33.80	-0.20	96 000.00	4.00
	138.60	-1.40	572 000.00	5.00
	-15.30	2.20	154 000.00	16.00
51	-13.90	2.00	132 000.00	15.00
	102.90	14.70	786 500.00	12.00
	-15.30	0.00	227 000.00	19.00
	-13.90	0.00	195 000.00	18.00
50	102.90	0.00	1 158 000.00	14.00

All these criteria have different units that make normalization necessary to make comparisons. The normalized decision making matrix for SAW and MEW methods is determined according to formulas (1), (2), (3), (4), (5) and (6) and is presented in Table 6.

 Table 6. Normalized decision-making matrix (SAW and MEW methods)

		Crit	teria	
A 14 anna a tir a	<i>x</i> <sub>1</sub>	<i>x</i> <sub>2</sub>	<i>x</i> <sub>3</sub>	<i>x</i> <sub>4</sub>
Alternative		Optimizatio	on direction	
	min	min	min	min
$A_1$	0.0149	0.0015	0.4000	0.2857
$A_2$	0.0282	0.0030	0.2400	0.3333
$A_3$	0.1959	0.0283	0.0296	0.2857
$A_4$	0.0671	0.0075	0.0147	0.0513
$A_5$	0.0682	0.0008	0.0206	0.0714
$A_6$	0.1730	0.0283	0.0048	0.0435
$A_7$	0.0688	0.0075	0.0225	0.0800
A <sub>8</sub>	0.0818	0.0075	0.0222	0.0909
$A_9$	0.3881	0.0642	0.0036	0.0741
A <sub>10</sub>	0.0121	0.0000	0.4390	0.2857
A <sub>11</sub>	0.0165	0.0000	0.5106	0.4000
A <sub>12</sub>	0.0733	0.0075	0.1008	0.4000
A <sub>13</sub>	0.0552	0.4173	0.0554	0.1176
A <sub>14</sub>	0.0656	0.4545	0.1029	0.2500
A <sub>15</sub>	0.3474	0.2149	0.0200	0.2222
A <sub>16</sub>	0.0741	0.4173	0.0600	0.1818
A <sub>17</sub>	0.0875	0.4545	0.1029	0.4000
A <sub>18</sub>	0.4686	0.2158	0.0200	0.4000
A <sub>19</sub>	0.1417	0.2234	0.0240	0.0714
A <sub>20</sub>	0.1727	0.1984	0.0248	0.0870
A <sub>21</sub>	1.0000	0.0531	0.0050	0.1111
A <sub>22</sub>	0.0236	0.0075	0.8571	1.0000
A <sub>23</sub>	0.0289	0.0075	1.0000	1.0000
A <sub>24</sub>	0.1185	0.0528	0.1674	1.0000
A <sub>25</sub>	0.0106	0.0000	0.3214	0.1818
A <sub>26</sub>	0.0085	0.0000	0.3750	0.1667
A <sub>27</sub>	0.0629	0.0000	0.0629	0.2000
A <sub>28</sub>	0.0236	0.0075	0.3214	0.4000
A <sub>29</sub>	0.0289	0.0075	0.3750	0.5000
A <sub>30</sub>	0.1185	0.0528	0.0629	0.4000
	0.0131	0.4801	0.2338	0.1250
A_{32}	0.0119	0.4818	0.2727	0.1333
<u>32</u>	0.0880	0.3914	0.0458	0.1667
	0.0131	0.0000	0.1586	0.1053
A <sub>35</sub>	0.0119	0.0000	0.1846	0.1111
A <sub>36</sub>	0.0880	0.0000	0.0311	0.1429

When using the COPRAS method, normalization was made by applying the algorithm in equation (7) after all values, including  $x_{ij} < 0$ ,  $\forall -\infty \le x_{ij} \le \infty$ , were transformed into positive values.

All weighted and normalized values from calculations employing SAW, MEW and COPRAS methods are presented in Tables 7, 8 and 9 for each separate building.

This table also presents optimality criteria calculated for each of the methods using equations (8), (9) and (10) respectively. These criteria show the weight of each alternative. The highest value means the best alternative.

According to the results of the SAW method, the most preferred solution to the renovation method for all (B1), (B2) and (B3) buildings is additional thermal insulation in the attic. On the contrary, according to MEW and COPRAS methods, the most preferred alternative for all three buildings is the adjustment of a heating system and valves in thermostats.

Name of action	Weighted-normalized matrix of SAW method			Weig	_	nalized mat method	rix of	Weighted-normalized matrix of COPRAS method				>	N	RAS		
		<i>x</i> <sub>1</sub>	<i>x</i> <sub>2</sub>	<i>x</i> <sub>3</sub>	<i>x</i> <sub>4</sub>	<i>x</i> <sub>1</sub>	<i>x</i> <sub>2</sub>	<i>x</i> <sub>3</sub>	<i>x</i> <sub>4</sub>	<i>x</i> <sub>1</sub>	<i>x</i> <sub>2</sub>	<i>x</i> <sub>3</sub>	<i>x</i> <sub>4</sub>	SAW	MEW	COPRA
Attic insulation	$A_1$	0.0016	0.0004	0.0748	0.1343	0.6375	0.2159	0.8425	0.5550	0.0004	0.0035	0.0004	0.0063	0.2110	0.0643	0.0335
Facade insulation	$A_4$	0.0072	0.0018	0.0027	0.0241	0.7490	0.3156	0.4542	0.2476	0.0017	0.0035	0.0097	0.0350	0.0358	0.0266	0.0087
Windows and doors	$A_7$	0.0074	0.0008	0.0024	0.0086	0.7510	0.3156	0.4919	0.3051	0.0017	0.0035	0.0063	0.0224	0.0191	0.0356	0.0122
Tightening windows and doors	$A_{10}$	0.0013	0.0000	0.0470	0.0306	0.6233	0.0000	0.8573	0.5550	0.0003	0.0035	0.0003	0.0063	0.0788	0.0000	0.0336
Recovery 60%	$A_{13}$	0.0059	0.0447	0.0059	0.0126	0.7335	0.8136	0.5821	0.3657	0.0014	0.0049	0.0026	0.0152	0.0691	0.1271	0.0162
Recovery 80%	$A_{16}$	0.0079	0.0447	0.0064	0.0195	0.7569	0.8136	0.5909	0.4488	0.0019	0.0049	0.0024	0.0099	0.0785	0.1633	0.0215
Heat pump	$A_{19}$	0.0152	0.0239	0.0026	0.0076	0.8113	0.7021	0.4979	0.2893	0.0036	0.0122	0.0059	0.0251	0.0493	0.0820	0.0113
Adjust heat system	A <sub>22</sub>	0.0025	0.0008	0.0917	0.1070	0.6697	0.3156	0.9716	1.0000	0.0006	0.0035	0.0002	0.0018	0.2020	0.2054	0.0623
Individual metering tap water	A <sub>25</sub>	0.0011	0.0000	0.0344	0.0195	0.6148	0.0000	0.8088	0.4488	0.0003	0.0035	0.0004	0.0099	0.0550	0.0000	0.0246
Individual metering heat	A <sub>28</sub>	0.0025	0.0008	0.0344	0.0428	0.6697	0.3156	0.8088	0.6501	0.0006	0.0035	0.0004	0.0045	0.0805	0.1111	0.0406
Solar collectors	$A_{31}$	0.0014	0.0514	0.0250	0.0134	0.6288	0.8410	0.7620	0.3763	0.0003	0.0038	0.0006	0.0144	0.0912	0.1516	0.0183
Water taps	A <sub>34</sub>	0.0014	0.0000	0.0170	0.0113	0.6288	0.0000	0.7087	0.3471	0.0003	0.0035	0.0009	0.0170	0.0296	0.0000	0.0160

Table 7. Weighted-normalized	decision-making matrix and	optimal results of building 1 (	(B1)

Name of action		Weighted-normalized matrix of SAW method				Weig	Weighted-normalized matrix of MEW method				Weighted-normalized matrix of COPRAS method				M	COPRAS
		<i>x</i> <sub>1</sub>	<i>x</i> <sub>2</sub>	<i>x</i> <sub>3</sub>	$x_4$	<i>x</i> <sub>1</sub>	<i>x</i> <sub>2</sub>	<i>x</i> <sub>3</sub>	<i>x</i> <sub>4</sub>	<i>x</i> <sub>1</sub>	<i>x</i> <sub>2</sub>	<i>x</i> <sub>3</sub>	<i>x</i> <sub>4</sub>	SAW	MEW	COF
Attic insulation	$A_2$	0.0030	0.0007	0.0449	0.1567	0.6827	0.2542	0.7658	0.5967	0.0007	0.0035	0.0006	0.0054	0.2053	0.0793	0.0362
Facade insulation	$A_5$	0.0073	0.0002	0.0038	0.0336	0.7503	0.1833	0.4837	0.2893	0.0017	0.0035	0.0069	0.0251	0.0449	0.0192	0.0112
Windows and doors	$A_8$	0.0088	0.0008	0.0024	0.0097	0.7650	0.3156	0.4905	0.3240	0.0021	0.0035	0.0064	0.0197	0.0217	0.0384	0.0134
Tightening windows and doors	$A_{11}$	0.0018	0.0000	0.0546	0.0428	0.6446	0.0000	0.8819	0.6501	0.0004	0.0035	0.0003	0.0045	0.0992	0.0000	0.0411
Recovery 60%	$A_{14}$	0.0070	0.0486	0.0110	0.0268	0.7471	0.8302	0.6536	0.5212	0.0017	0.0042	0.0014	0.0072	0.0934	0.2113	0.0280
Recovery 80%	$A_{17}$	0.0094	0.0486	0.0110	0.0428	0.7705	0.8302	0.6536	0.6501	0.0022	0.0042	0.0014	0.0045	0.1118	0.2718	0.0355
Heat pump	A <sub>20</sub>	0.0185	0.0212	0.0027	0.0093	0.8287	0.6826	0.5010	0.3173	0.0043	0.0142	0.0057	0.0206	0.0517	0.0899	0.0126
Adjust heat system	A <sub>23</sub>	0.0031	0.0008	0.1070	0.1070	0.6844	0.3156	1.0000	1.0000	0.0007	0.0035	0.0001	0.0018	0.2179	0.2160	0.0627
Individual metering tap water	A <sub>26</sub>	0.0009	0.0000	0.0401	0.0178	0.6002	0.0000	0.8324	0.4308	0.0002	0.0035	0.0004	0.0108	0.0589	0.0000	0.0232
Individual metering heat	A <sub>29</sub>	0.0031	0.0008	0.0401	0.0535	0.6844	0.3156	0.8324	0.7220	0.0007	0.0035	0.0004	0.0036	0.0975	0.1298	0.0458
Solar collectors	$A_{32}$	0.0013	0.0516	0.0292	0.0143	0.6223	0.8417	0.7843	0.3879	0.0003	0.0038	0.0005	0.0135	0.0963	0.1594	0.0193
Water taps	$A_{35}$	0.0013	0.0000	0.0198	0.0119	0.6223	0.0000	0.7291	0.3560	0.0003	0.0035	0.0008	0.0161	0.0329	0.0000	0.0168

Table 8. Weighted-normalized decision-making matrix and optimal results of building 2 (B2

Name of action	Weighted-normalized matrix of SAW method		Weig		nalized mat method	rix of	Weighted-normalized matrix of COPRAS method				7	N	RAS			
		<i>x</i> <sub>1</sub>	<i>x</i> <sub>2</sub>	<i>x</i> <sub>3</sub>	<i>x</i> <sub>4</sub>	<i>x</i> <sub>1</sub>	<i>x</i> <sub>2</sub>	<i>x</i> <sub>3</sub>	<i>x</i> <sub>4</sub>	<i>x</i> <sub>1</sub>	<i>x</i> <sub>2</sub>	<i>x</i> <sub>3</sub>	<i>x</i> <sub>4</sub>	SAW	MEW	COPRA
Attic insulation	$A_3$	0.0210	0.0067	0.0055	0.1343	0.8399	0.4312	0.5179	0.5550	0.0049	0.0034	0.0048	0.0063	0.1675	0.1041	0.0281
Facade insulation	$A_6$	0.0185	0.0067	0.0009	0.0204	0.8288	0.4312	0.3690	0.2291	0.0044	0.0034	0.0295	0.0413	0.0465	0.0302	0.0089
Windows and doors	$A_9$	0.0415	0.0069	0.0004	0.0079	0.9037	0.5230	0.3498	0.2943	0.0098	0.0033	0.0393	0.0242	0.0567	0.0487	0.0148
Tightening windows and doors	$A_{12}$	0.0078	0.0008	0.0108	0.0428	0.7561	0.3156	0.6511	0.6501	0.0018	0.0035	0.0014	0.0045	0.0622	0.1010	0.0377
Recovery 60%	$A_{15}$	0.0372	0.0230	0.0021	0.0238	0.8930	0.6957	0.4812	0.4932	0.0087	0.0129	0.0071	0.0081	0.0861	0.1474	0.0207
Recovery 80%	$A_{18}$	0.0501	0.0231	0.0021	0.0428	0.9221	0.6964	0.4812	0.6501	0.0118	0.0128	0.0071	0.0045	0.1182	0.2009	0.0256
Heat pump	A <sub>21</sub>	0.1070	0.0057	0.0005	0.0119	1.0000	0.0000	0.0000	0.0000	0.0252	0.0629	0.0283	0.0161	0.1251	0.0000	0.0283
Adjust heat system	A <sub>24</sub>	0.0127	0.0057	0.0179	0.1070	0.7960	0.4996	0.7159	1.0000	0.0030	0.0033	0.0009	0.0018	0.1433	0.2847	0.0593
Individual metering tap water	A <sub>27</sub>	0.0067	0.0000	0.0067	0.0214	0.7437	0.0000	0.5962	0.4693	0.0016	0.0035	0.0023	0.0090	0.0349	0.0000	0.0244
Individual metering heat	$A_{30}$	0.0127	0.0057	0.0067	0.0428	0.7960	0.4996	0.5962	0.6501	0.0030	0.0033	0.0023	0.0045	0.0679	0.1541	0.0364
Solar collectors	A <sub>33</sub>	0.0094	0.0419	0.0049	0.0178	0.7710	0.8014	0.5617	0.4308	0.0022	0.0055	0.0031	0.0108	0.0740	0.1495	0.0196
Water taps	$A_{36}$	0.0094	0.0000	0.0033	0.0153	0.7710	0.0000	0.5225	0.4007	0.0022	0.0035	0.0046	0.0126	0.0280	0.0000	0.0185

Table 9. Weighted- normalized	decision-making matrix and	optimal results of building 3 (B3)
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According to the MEW method, the obtained results also showed that the owners would prefer heat recovery from ventilation air with regenerative heat exchangers having 80% efficiency. When comparing all results, we can state that the most preferred measure for the renovation of this group of facility owners is the adjustment of a heating system and valves in the thermostat, because MEW and COPRAS disclosed the best results of preferences for this alternative; the application of the SAW method also shows good results of this renovation measure.

For all buildings and decision making methods, the adjustment of heating systems come high up on the list. In this case, one of the reasons might be short pay backtime which is prioritized by the building owners. It is, however, doubtful if this action really should be considered a renovation method while it is more likely to be ordinary upkeep. Tightening windows and doors and changing water taps into more efficient ones should also be included in normal upkeep. Individual metering for heating and hot tap water will certainly influence energy consumption of the building; however, it is something more related to the user's behaviour than to the properties of the building.

Additional thermal insulation in the attic and on facades, the installation of new windows, doors and equipment for heat recovery using heat exchangers or a heat pump are, however, real investments that reduce the use of energy in buildings in different ways.

When limiting views on alternatives that are not only ordinary upkeep, the results will be slightly different. Calculations will remain valid because in any selection of alternatives those with the highest values are the ones that should be chosen.

If one method for heat recovery is selected, the other two will not be applicable. Thus, in that case, only thermal insulation in the attic or on facades as well as new doors and windows will remain as alternatives.

For all three buildings and for almost all decision methods, "heat recovery of 80%" falls out as the best or second best option with regard to the preferences of building owners.

Additional thermal insulation in the attic always falls out with high priority in the limited selection of remaining alternatives when one method of heat recovery is chosen.

Rather short pay back-times characterize the actions that come first when multi criteria decision methods are applied to the data obtained. Nevertheless, we should not forget that these calculations are made according to the owner's opinion.

This result could mean that there is not enough information and motivation for the dwellers about energy savings. They only care about having a short payback period. Information or subsidiaries (or even taxation) could motivate building owners to take care more about energy savings and Global Warming Potential (GWP) situation in the world.

If a decision maker wants to know the least desirable solution, s/he has to refer to the results of COPRAS and SAW methods, because a general action of the MEW method is multiplication, and this is the case why some of the results equal to 0. However, it does not mean that this result is the worst.

These calculations can be helpful from some other aspects because when using them we can make choices not only between all alternatives in the matrix but also between two or three of the alternatives. If the building owner has a limited amount of money, these calculations can help him with choosing the most attractive presented solution.

For example, if the owner wants to add more thermal insulation and s/he is hesitant when choosing between the alternatives to put it in the attic or on facades, we can state that the most preferable solution is additional thermal insulation in the attic (see Tables 7, 8 and 9; the results of alternatives 1 to 6).

If the owner is going to either change his/her windows and doors or tight around the windows, we can accept that the best solution, according to the opinion of the owner, is tightening around the window (see Tables 7, 8 and 9; the results of alternatives 7 to 12).

Moreover, if the owner decided to renovate the ventilation system, choosing between solutions to recover 60% of heat from exhaust air with plate heat exchangers, 80% of heat from exhaust air with regenerative heat exchangers and by using a heat pump to take heat from exhaust air, the result shows that the best alternative is the regenerative heat exchanger giving recovery of 80% of heat from exhaust air (see Tables 7, 8 and 9; the results of alternatives 13 to 21).

# 4. Conclusions

1. Three building apartments built in residential areas in the '50s, '60s and '70s were selected. For each of these buildings, a series of energy calculations have been done using E-norm energy calculation software. The best alternatives for all above introduced building apartments were selected using multi-criteria decision making methods.

2. This determination was made according to recommendations produced by Simple Additive Weighting (SAW), Multiplicative Exponential Weighting (MEW) and Complex Proportion Assessment (COPRAS) methods. The obtained results point to the usefulness of combining different multi-criteria decision making methods, because in this case, the decision maker can compare results that are not always the same.

3. According to the achieved results, the best alternative was adjusting the heating system and valves in thermostats. The cost of adjusting the heating system is supposed to give savings because the average temperature in the building can decrease in 1 °C. This alternative was chosen because of the short payback period, which, as the results showed, was very important for building owners.

4. When limiting choices for the above mentioned renovation actions that cannot be considered to be normal, upkeep heat recovery from ventilation air and additional thermal insulation in the attic fall out to be quite attractive for building owners.

5. The opinion of the decision maker has a big impact on the results. In this case study, building owners gave a lot of votes for the payback period. Thus, the obtained results also showed the best solution like an alternative to the shortest payback period.

6. The received results show it is necessary to inform and motivate the dwellers about the energy consumption problem and help them with becoming more motivated about their needs with reference to the Global Worming problem in the world.

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# SAVININKŲ TEIKIAMI PRIORITETAI PASTATŲ ATNAUJINIMO PRIEMONĖMS: DAUGIAKRITERINIŲ SPRENDIMO PRIĖMIMO METODŲ TAIKYMO PAVYZDYS

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#### Santrauka

Straipsnyje išnagrinėti trys tipiniai švedų daugiabučiai, pastatyti 6-ajame, 7-ajame ir 8-ajame dešimtmečiais. Buvo atlikti kiekvieno šių pastatų atnaujinimo priemonių skaičiavimai, įvertinantys efektyvumą ir investavimo apimtis, kuriomis siekiama didinti energijos vartojimo efektyvumą. Taikant daugiakriterinius sprendimo priėmimo metodus, tokius kaip *Simple Additive Weighting* (SAW), *Multiplicative Exponential Weighting* (MEW) and *COmplex PRoportion ASsessment* (COPRAS), buvo tiriami savininkų teikiami prioritetai pastatų atnaujinimo priemonėms. Tyrimas buvo atliekamas vertinant keturis pastatų kriterijus: energija, vartojama centralizuotam šildymui, ir elektros energija, investicijų sąnaudos ir atsipirkimo laikotarpis. Atlikus skaičiavimus buvo nustatyta, kad didelę įtaką tyrimo rezultatams daro savininkų nuomonė. Šie savininkai daugiausia dėmesio skyrė trumpam renovacijos priemonių atsipirkimo laikotarpiu. Viena patrauklesnių renovacijos priemonių yra papildoma šilumos izoliacija palėpėje ir šilumos gavimas iš ištraukiamo oro.

**Reikšminiai žodžiai**: energinis efektyvumas, rangavimas, stambiaplokščiai namai, atnaujinimas, SAW, MEW, COPRAS, AHP metodai, MCDM.

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