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THE APPLICATION OF THE LINDO PROGRAM TO SOLVING LOCATION PROBLEMS FOR CONCRETE MIX PRODUCTION PLANTS

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1. Introduction

Problem of location belongs to the oldest optimization task in construction industry. It appears cyclically, according to the needs, new approaches, and new solution methods of this problem (cf. Soderman [1], Skibicki [2], Daellenbach et al. [3], Harris & McCaffer [4], Francis & White [5], Kruse et al. [6]).

Therefore, there are many aspects of this problem. Let us mention the most characteristic ones and some examples:

- personnel management (personnel transfer problem) - cf. Wright et al. [7],
- optimal placement of buildings, eg Baskaran & Statopoulos [8],
- arrangement of accommodations, eg Riopel & Langevin [9],
- public investment and capital allocation, eg Georgi [10], Weingartner [11], Nemhauser & Ullman [12],
- transport infrastructure location (in context: site planning), eg Olszewski [13], Prystupa [14],
- municipal management planning problems, such as:
  - location of municipal objects, eg Huang et al. [15], Wijeratne & Wirasinghe [16],
  - environmental and regional planning - see: Meester [17], Suh et al. [18],
- location of prefabrication plants - see: Warszawski [19, 20, 21], Warszawski & Ishai [22].

Separate aspects of this question are the location problems of the facilities on building site, eg Kamiński [23], Lennerts & Knauer [24], Warszawski & Peer [25].

Also, the planning of elements required for the management of a construction site for modernisation and investment purposes is a complicated process based on a proper understanding of contemporary trends. These problems require a unified technical-technological, organisational, utilitarian and economic approach. Under such conditions, methods utilising optimisation procedures are called for as these approaches should increase management effectiveness.

This paper presents a methodology for solving the location problems for a concrete mix plant based on prognoses of demand for concrete mix. It includes a method for calculating these quantities and deals with fundamental problems concerning the modelling of concrete mix plant location problems. Particular attention has been paid to the choice of a proper mathematical model and its solution. The paper is illustrated throughout with optimisation formulas for Poznań (Poland) and its environs - 700,000 inhabitants.

2. Methodology for setting demand quantities of concrete mix

A question posing considerable difficulties is that of arriving at prospective demand quantities for concrete mix within a given region and in a defined time span.

Hitherto employed quantities considered in location problems have been obtained from the daily production records of individual concrete mix plants on an "ex post facto" basis. Accordingly, wrong decisions undertaken, additional costs accruing to investors etc could be determined. Due, however, to the unique nature of the construction industry, the dispersal and variety of investment projects and the variability of demand quantities for concrete mix, the quantities obtained by the above means needn't be appropriate in future situations.

Solution of location problems demands the ability to make accurate prognoses of future demand quantities. An attempt at making such prognoses is found in basing them on demand indices for concrete mix. Fig 1 illustrates the functioning algorithm. The basis for ascertaining the magnitude of the concrete mix demand indices was data obtained from technical documentation, technological and work organisation plans as well as cost estimates.
Initial Data:
- technical documentation
- technological and organisational plan
- cost estimates and calculations

Classification of buildings according to their construction characteristics and intended function

Determination of concrete mix to be built into individual stages of the building under construction

Calculation of indices \((W)\) for concrete mix demand

\[ W_{Ab} = \frac{M}{A_{build}} \text{ m}^3/\text{m}^2; \quad W_v = \frac{M}{V} \text{ m}^3/\text{m}^3 \]

\[ W_{Ag} = \frac{M}{A_{gross}} \text{ m}^3/\text{m}^2; \quad W_{ko} = \frac{M}{K_o} \text{ m}^3/\text{PLN} \]

Verification of results (correlation calculations)

Choice of optimal index

Developmental plans

Construction phases

Investor's decision

Determination of concrete mix demand within the given region and at a given time

Fig 1. Algorithm for obtaining the given amount of concrete mix demanded: \(M\) - amount of concrete mix \([\text{m}^3]\); \(A_{build}\) - area of building \([\text{m}^2]\); \(A_{gross}\) - gross area \([\text{m}^2]\); \(V\) - volume of building \([\text{m}^3]\); \(K_o\) - estimated value \([\text{PLN}]\)

It is on the basis of the above values, at each of the specific stages of the buildings' construction, that the amount of concrete mix built into the structure was determined. Demand indices determine the amount of concrete mix built into the individual stages of the buildings being constructed for each \(1 \text{ m}^3\) of the building volume per \(1 \text{ m}^2\) of the area under construction, each \(1 \text{ m}^3\) of the gross area and each \(1\)-PLN of estimated value (\(\text{£} 5.0 \text{ PLN}\)). Separation into individual construction phases permits the demand for concrete mix to be determined within the time of the completed construction (cf Powell, [26]).

The determined value of the demand indices for concrete mix based on the building area and the gross area of buildings considered showed a significant dispersion of results. These must, consequently, be deemed as unreliable. Due to a sizeable rate of inflation (as exists in Poland), an attempt to determine the relationship between the amount of concrete mix built into individual buildings and its value in preliminary estimates was unsuccessful. It is, however, possible to determine future demand for concrete mix based on demand indices related to the volume of buildings. The statistical analysis conducted on individual buildings allowed for a determination of average values and standard deviation values. Values of concrete mix demand indices were determined on the basis of amounts obtained for 326 buildings.

The purpose of the buildings, the kind of construction they represented allowed the groups of buildings shown in Fig 2 to be analysed. Correlation showed linear dependencies between the amount of concrete mix built into the structure and the volume of the structure itself. Buildings having a larger overall volume showed smaller concrete mix demand indices. For those buildings where no functional dependence was found, average values (\(\mu\)), standard deviations \((S)\) and variation coefficients \((v)\) were determined.

Fig 3 presents values for certain groups of buildings.
Introducing the values of concrete mix demand at the preliminary design stage of a project permits determination of the projected demand for concrete mix. The balance of these values together with the practical capacity of a production plant allows for a calculation of the required number of plants.

### 3. The modelling of concrete mix plant location problems

A number of modelling methods dealing with location problems are found in the literature, e.g. procedures branch and bound (Warszawski, [20]), graph theory (Woźnica, [27]), fuzzy dynamic programming (Huang et al., [15]) and those dealing with uncertainty conditions (Kamiński, [23]). The approach presented in the article is based on projected amounts of concrete mix demand with a non-linear cost-production function for concrete mix.

A number of options concerning the location of concrete mix plants are considered. The creation of such location options demands the consideration of a number of factors having different values which are not always open to mathematical expression. The prime location factors concerning the individual elements of the production line are presented in Fig 4. They were considered in the creation of a so-called function criterion as well as limiting conditions. The article presents only a generalised form of the model based on the production costs of raw materials, their transport, costs of production and transport of concrete mix and plant construction and installation costs.

The function criterion has the form:

$$K_c = \sum_{z\in\mathcal{Z}} (c_z + k_z)Q_z + \sum_{p\in\mathcal{P}} (c_p + k_p)Q_p + \sum_{b\in\mathcal{B}} k_b \rightarrow \min,$$

- $c_z$ - unit purchase cost of a given ingredient for concrete mix,
- $k_z$ - unit cost of transport for raw materials for concrete mix,
- $Q_z$ - amount of purchased raw materials,
- $c_p$ - unit cost of producing 1 m$^3$ of concrete mix,
- $k_p$ - unit cost of transporting 1 m$^3$ of concrete mix,
- $Q_p$ - amount of concrete mix produced,
- $k_b$ - costs of building plants at alternative sites.

The proposed mathematical model for solving the problem of localising concrete mix plants and its limitations has been presented by Celinski [28]. This model has been verified by Jagla [29] as well. The model introduces two kinds of variables:

- $X_i$ describing the amount of concrete mix produced in the $i$-th location and destined to the $j$-th demand site.
- $Y_j$ describing the location site of the concrete mix plant; this variable may assume the binary value (0,1) concerning the given location site.
Fig 3. Values of concrete mix demand indices for selected types of buildings
The model introduces 10 constraining conditions concerning the location and amount of raw materials produced, location and practical production capacity of concrete mix plants, and location and amount of concrete mix demanded. The assumptions of this model allowed for the change of multi-extreme and non-linear problem into integer one. The proposed method for describing the optimal number of concrete plant location sites is presented in Fig 5.

### 4. Examples of data analysis

The data analysis was conducted on calculations for Poznań and its environs. This allowed finding answers to the following questions:

- how many and on what sites of the area considered should there be installed concrete mix plants of a given capacity,
- how much concrete mix should be transported to certain demand sites from given production plants.

The data analysis was based on anticipated amounts of concrete mix needed obtained on the basis of concrete mix demand indices and plans for expanding building construction in the area considered. The production amounts were based on the practical capacities for manufacturing concrete mix. Location sites of currently functioning plants as well as location sites for alternate plants were considered.

Within the given area, the following were indicated:

- 87 concrete mix demand sites (within 0.5 km from the demand site, a sum total of demand was assumed),
- 14 concrete mix production sites,
- 12 alternate plant location sites,
- 2 levels of practical concrete mix production capacity, ie 31,000 m³/year and 37,000 m³/year.

Levels were set for various seasonal indices, reliability of plant facilities and irregularity of demand for concrete mix.

Alternative sites of plant location were obtained by means of the division method (Kopociński, [30]) by selecting out subdivisions of the Poznań area where concrete mix plants could be located. The basis of the scale was a grid having side of 2 km. Topographical analysis allowed for a precise location in specific areas where plants could be localised. The process of calculation included purchase costs of obtaining raw materials, the costs of production within the function of production capacity, costs of transporting the concrete mix from all production sites to demand sites.

Calculations were performed utilising standard software (Lindo, [31]) for discrete programming.
The Lindo System Inc. - 1984 program [31] was developed for the purpose of offering solutions to problems based on integer programming and quadratic programming. Seeking optimal locations for concrete mix production sites was conducted on the basis of the program version concerning integer programming (according to a mathematical model). In the first stage numerical programming, the output data was prepared its appropriate use in the numerical process. The Lindo program operates on data matrices introduced into equations concerning limiting parameters and boundary conditions. A significant improvement of the computing process is achieved through the method of branch and bound. Such a solution, in a decided way, shortens and simplifies numerical computation.

The application of the Lindo program and discrete programming allowed for a description of location sites for production plants and the division of production capacity over a period of 3 years. The necessary production capacity thus obtained allowed for a choice of parameters and kinds of production facilities. These calculations were performed for 104 location situations. Optimal values obtained on the basis of calculations are presented in Table 1. These include minimal values of costs at given practical plant production levels as well as differences between extreme location options.

Table 1 presents minimal values of criterion functions for horizontally presented practical production capacities of plants, ie 37,000 m$^3$ and 31,000 m$^3$ (per year), respectively. The given optimal sites were located as was the number of plants for minimal values of criterion functions (column 5). As well, the calculated percent differences between minimal and maximal values of the criterion function under the considered conditions are presented (column 6).
Table 1. Results of optimal situations

<table>
<thead>
<tr>
<th>No</th>
<th>Time Periods</th>
<th>Values of the Criterion Function [PLN]</th>
<th>Level of Practical Production Capacity [m³/year]</th>
<th>Optimal Number of Production Plants</th>
<th>Percent Differences Between Values of Criterion Functions</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>Year I</td>
<td>55,743.37</td>
<td>37,000</td>
<td>4</td>
<td>32.0</td>
</tr>
<tr>
<td></td>
<td></td>
<td>57,882.80</td>
<td>31,000</td>
<td>5</td>
<td>29.5</td>
</tr>
<tr>
<td>2.</td>
<td>Year II</td>
<td>62,102.78</td>
<td>37,000</td>
<td>5</td>
<td>26.0</td>
</tr>
<tr>
<td></td>
<td></td>
<td>66,906.17</td>
<td>31,000</td>
<td>5</td>
<td>27.8</td>
</tr>
<tr>
<td>3.</td>
<td>Year III</td>
<td>64,416.13</td>
<td>37,000</td>
<td>3</td>
<td>33.0</td>
</tr>
<tr>
<td></td>
<td></td>
<td>54,509.75</td>
<td>31,000</td>
<td>2</td>
<td>28.0</td>
</tr>
</tbody>
</table>

In the first phase, the optimal number of concrete mix plants was 4, at a level of 37,000 m³ of practical production capacity and 5, at a level of 31,000 m³. The differences obtained between the values of the criterion functions expressed as percentages were 32% and 29%, respectively. The change in location of demand points and their respective demand quantities in later phase allowed for an optimal realisation of production with fewer production plants. In phase III, this was 3 and 2, respectively.

5. Conclusions

1. The presented approach permits the programming of location sites for production plants at the preliminary design stage according to the specifications of the project brief. This procedure allows for the flexible functioning of enterprises responsible for the production of the transported concrete mix.

2. The presented demand indices for concrete mix are verification of the existing linear relationship between the amount of concrete used and the volume. The given indices may be employed for the purpose of organising construction (utilisation of materials, storage area) as well as simplified estimating procedures.

3. Finding location sites for concrete mix plants were based on a topographic assessment of the area. Such a mathematically formulated approach may be used in the solution of all manner of location questions. Consideration of topographic conditions allows for a choice of possible plant location sites. The choice of optimal sites results from optimisation calculations.

4. The proposed methodology supported by software allows for the solution of location problems for the remaining elements of the construction camp.

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LINDO PROGRAMA BETONO MAIŠYMO GAMYKLOS VIETAI PARINKTI

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